Ab Initio Investigation of the Electronic Structure and Rovibrational Spectroscopy of Group-I and II Metal Hydrides and Helides

A Thesis Presented for the Degree of Doctor of Philosophy

at

The University of Newcastle

by

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Declaration

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(Signed)		
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Alister James Page

2008

To Mardi and my family.

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Abstract

The electronic structure and rovibrational spectroscopy of MH_2 , MH_2^{n+} , $HMHe^{n+}$ and MHe_2^{n+} (M = Li, Be, Na, Mg, K, Ca; n=1, 2) have been investigated using correlated *ab initio* ansatz.

In order to determine the efficacy of various electronic structure methods with respect to Group-I and II hydrides and helides, atomic properties of Li, Be, Na, Mg, K and Ca were calculated. Relativistically-corrected UCCSD(T) and IC-MRCI(+Q) were deemed to be the most suitable ansatz with respect to both efficiency and accuracy. The lowest 2A_1 and $^2\Sigma^-$ states of $\mathrm{MH_2}$ were found to be purely repulsive, in agreement with previous predictions. The main factor determining the structure and stability of the excited states of MH₂ was the relative orientations and occupations of the valence p atomic orbital of M and the H_2 $1\sigma_u$ orbital. The ground states of MH_2^{n+} were found to be the result of the charge-quadrupole interaction between \mathbf{M}^{n+} and the \mathbf{H}_2 molecular subunit. The structures of the ground states of HMHe⁺ were extremely fluxional with respect to the central bond angle co-ordinate. The ground state PESs of MHe_2^+ were also extremely sensitive to the abinitio ansatz by which they are modelled. The respective bonding of the H and He in both HMHe⁺ and HMHe²⁺ appeared to be charge-dependent in the case of Be, Mg and Ca. Despite the weak bonding observed for the Group-II hydrohelide and helide monocations, the corresponding dications each exhibit thermodynamically stable equilibria.

The solution algorithm of von Nagy-Felsobuki and co-workers was employed in the calculation of vibrational and rovibrational spectra. This algorithm employed an Eckart-Watson Hamiltonian in conjunction with rectilinear normal co-ordinates.

Vibrational and rovibrational Hamiltonian matrices were diagonalised using variational methods. This algorithm was extended so that the vibration transition moment integrals, and hence vibrational radiative properties, of linear triatomic molecules could be calculated. A method by which vibration-averaged structures are calculated was also developed and implemented.

Analytical potential energy functions (PEFs) and dipole moment functions (DMFs) of $({}^{1}A_{1})LiH_{2}^{+}$, $({}^{1}A_{1})NaH_{2}^{+}$, $({}^{1}A_{1})BeH_{2}^{2+}$, $({}^{1}A_{1})MgH_{2}^{2+}$, $({}^{1}\Sigma_{g}^{+})BeHe_{2}^{2+}$, $({}^{2}\Sigma^{+})HBeHe^{2+}$, $({}^{1}\Sigma_{g}^{+})MgHe_{2}^{2+}$ and $({}^{2}\Sigma^{+})HMgHe^{2+}$ were developed using least-square regression techniques in conjunction with discrete *ab initio* grids. Vibrational structures and spectra of these species were subsequently calculated. In addition, the rovibrational spectra of $({}^{1}A_{1})LiH_{2}^{+}$, $({}^{1}A_{1})NaH_{2}^{+}$, $({}^{1}A_{1})BeH_{2}^{2+}$ and $({}^{1}A_{1})MgH_{2}^{2+}$ were calculated. For $({}^{1}A_{1})LiH_{2}^{+}$ and $({}^{1}A_{1})LiD_{2}^{+}$, calculated rovibrational transition frequencies for $J \leq 10$ and $0 \leq K \leq 3$ were within ca. 0.1-0.2% of experimental values.

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Table of Acronyms

ANO Atomic NO

ANO-RCC Relativistically corrected ANO basis set

AO Atomic orbital

aug-cc-pCVXZ Augmented cc-pCVXZ basis set

aug-cc-pVXZ Augmented cc-pVXZ basis set

aug-CVQZ Augmented CVQZ basis set

BO Born-Oppenheimer

BP Breit-Pauli

BSSE Basis set superposition error

CASSCF Complete active space SCF

CBS Complete basis set

cc Correlation consistent

cc-pCVXZ cc with polarisation, core and valence $X-\zeta$ basis set

cc-pVXZ cc with polarisation, valence X-ζ basis set

CC Coupled-cluster

CCSD CC with single and double excitations

CCSD(T) CCSD with perturbative treatment of triple excitations

CCSDT CCSD with 'full' triple excitations

CCSDT with quadruple excitations

CG Cowan-Griffin

CGTO Contracted GTO

CI Configuration interaction

CIS CI with single excitations

CISD CI with single and double excitations

CISDT CISD with 'full' triple excitations

CISDTQ CISDT with quadruple excitations

CVXZ Core-valence polarisation $X-\zeta$ basis set

Darw Relativistic Darwin correction

DFT Density functional theory

DHF Dirac-Hartree-Fock

DK Douglas-Kroll

 $\mathbf{DK}n$ n^{th} order DK correction

DMS Dipole moment surface

DMF Dipole moment function

DUN Dunham

 \mathbf{DZ} Double- ζ

ECP Effective core potential

EDUN Exponential Dunham

ESR Electron spin resonance

EOGL Exponential Ogilvie

ESPF Exponential Simons, Parr and Finlan

FCI Full CI

FEM Finite element method

FTIR Fourier Transform IR

GTO Gaussian type orbital

HEG Harris, Engerholm and Gwinn

HF Hartree-Fock

HOMO Highest occupied MO

IC-MRCI Internally contracted MRCI

IE Ionisation energy

 \mathbf{IE}_n n^{th} IE

IR Infra-red

LUMO Lowest unoccupied MO

MED Maximum electron density

MEP Minimum energy path

MCSCF Multi-configurational SCF

MO Molecular orbital

MP Møller-Plesset

 $\mathbf{MP}n$ n^{th} order Møller-Plesset

MP4(SDTQ) 'Full' MP4 with single, double, triple, quadruple excitations

MRCI Multi-reference CI

MRCISD MRCI with single and double excitations

MV Relativistic mass-velocity correction

NO Natural orbital

OGL Ogilvie

PES Potential energy surface

PEF Potential energy function

 $+\mathbf{Q}$ Davidson correction (viz. CISD+Q/MRCISD+Q)

QCI Quadratic CI

QCISD QCI with single and double excitations

QCISD(T) QCISD with perturbative treatment of triple excitations

 $\mathbf{Q}\mathbf{Z}$ Quadruple- ζ

RG Rare gas

RHF Spin-restricted HF

ROHF Spin-restricted open-shell HF

SCF Self consistent field

SD Slater determinant

SO Spin-orbit

SPF Simons, Parr and Finlan

SSFC Site-site function counterpoise

STO Slater type orbital

SVD Singular value decomposition

TM Transition metal

TZ Triple-ζ

UCCSD Spin-unrestricted CCSD

UCCSD(T) Spin-unrestricted CCSD(T)

UCCSDT Spin-unrestricted CCSDT

UHF Spin-unrestricted HF

UV Ultra-violet

VB Valence bond

VBO Vibration band origin

ZPE Zero-point energy